



Rewarding Learning

ADVANCED SUBSIDIARY (AS)  
General Certificate of Education  
2009

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## Mathematics

### Assessment Unit C2

*assessing*

Module C2: AS Core Mathematics 2

[AMC21]



FRIDAY 22 MAY, MORNING

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#### TIME

1 hour 30 minutes.

#### INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number on the Answer Booklet provided.

Answer **all eight** questions.

Show clearly the full development of your answers.

Answers should be given to three significant figures unless otherwise stated.

You are permitted to use a graphic or scientific calculator in this paper.

#### INFORMATION FOR CANDIDATES

The total mark for this paper is 75

Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

A copy of the **Mathematical Formulae and Tables booklet** is provided.

Throughout the paper the logarithmic notation used is  $\ln z$  where it is noted that  $\ln z \equiv \log_e z$

**Answer all eight questions.**

**Show clearly the full development of your answers.**

**Answers should be given to three significant figures unless otherwise stated.**

**1 (a) (i)** Simplify  $x(3x^2 + 2 + 4x^{-3})$  [1]

**(ii)** Hence, integrate with respect to  $x$

$$x(3x^2 + 2 + 4x^{-3})$$
 [4]

**(b)** Using the trapezium rule with 6 ordinates, find an approximate value for

$$\int_0^1 \frac{4}{(1+x^2)} dx$$
 [6]

**2 (i)** A sequence is defined recursively by

$$u_{n+1} = \frac{2}{3}u_n \quad \text{where } u_1 = 1$$

Find  $u_2, u_3$  and  $u_4$  [1]

**(ii)** State whether this sequence is convergent or divergent. [1]

A geometric series is formed by adding the terms of the sequence to give

$$1 + \frac{2}{3} + \frac{4}{9} + \frac{8}{27} + \dots$$

**(iii)** Find the common ratio of this geometric series. [1]

**(iv)** Find the sum to infinity of this geometric series. [2]

**3** In the binomial expansion of  $(1 + nx)^{10}$ , the coefficient of  $x^2$  is 3 times the coefficient of  $x$ .

Find the value of  $n$ , where  $n \neq 0$  [6]

- 4 (i) On the same diagram, sketch the curves  $y = 2^x$  and  $y = 1 + 2^x$ .  
Label any relevant points on the axes. [4]

The  $y$  coordinate of a point P on the curve  $y = 1 + 2^x$  is 6

- (ii) By solving the equation

$$1 + 2^x = 6$$

find the  $x$  coordinate of P.

[A solution by trial and improvement is not acceptable] [4]

- 5 (a) Prove the identity

$$\tan \theta + \frac{1}{\tan \theta} \equiv \frac{1}{\sin \theta \cos \theta} \quad [5]$$

- (b) Solve the equation

$$\sin^2 x = \frac{1}{4}$$

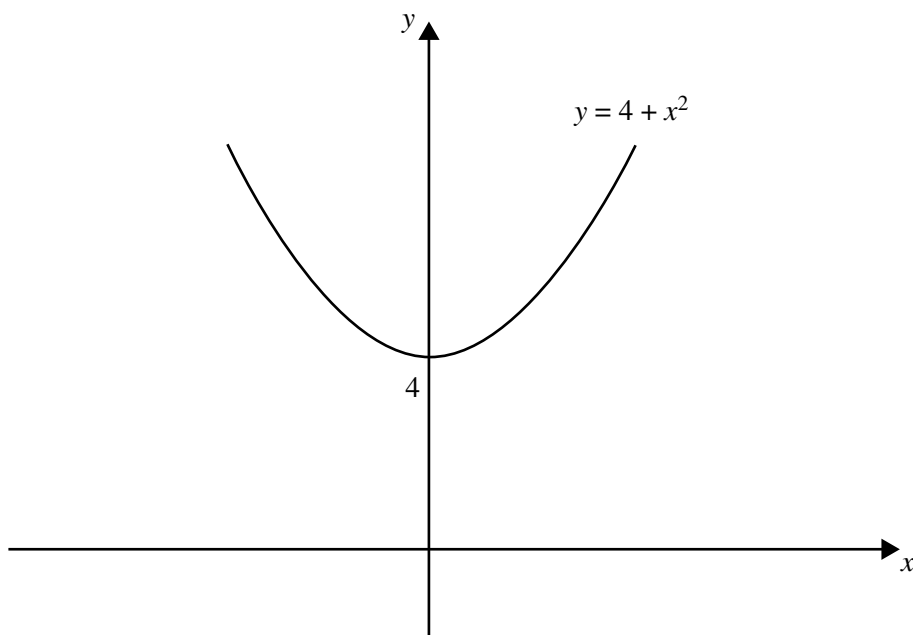
for  $-90^\circ < x \leq 90^\circ$  [4]

- (c) Solve the equation

$$\cos 2x = 0.4$$

for  $0 < x \leq \pi$  [4]

6 Shown in **Fig. 1** below is the curve  $y = 4 + x^2$



**Fig. 1**

- (i) Find the area of the region bounded by the curve  $y = 4 + x^2$ , the  $x$ -axis,  $y$ -axis and the line  $x = 1$  [5]
- (ii) Hence, find the area of the region bounded by the curve  $y = 4 + x^2$  and the line  $y = 5$  [4]

- 7 The network coverage of a mobile phone mast M may be modelled as a circle as shown in Fig. 2 below.

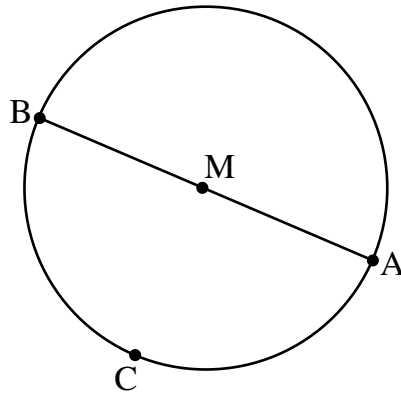


Fig. 2

Points A (2, 1), B( $k$ ,  $k + 5$ ) and C (-1, -1) lie on the circumference of the circle, centre M. AB is a diameter of the circle.

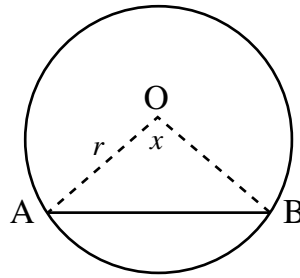
(i) Find the gradient of AC. [2]

(ii) Hence, write down the gradient of BC and **prove** that  $k = -3$  [4]

(iii) Find the equation of the circle in the form

$$(x - a)^2 + (y - b)^2 = r^2 \quad [5]$$

- 8 A silver medal is divided into two parts by a line AB.  
The medal is in the shape of a circle, centre O, as shown in **Fig. 3** below.



**Fig. 3**

The radius of the circle is  $r$  and the angle AOB is  $x$  radians.

(i) Write down the area of the minor sector OAB. [1]

(ii) Write down the area of the triangle AOB. [1]

The areas of the two parts of the medal divided by the line AB are in the ratio 5 : 1

(iii) Show that

$$\sin x = x - \frac{\pi}{3} \quad [8]$$

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**THIS IS THE END OF THE QUESTION PAPER**

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