Cambridge Assessment International Education

# Cambridge IGCSE™

**ADDITIONAL MATHEMATICS** **0606/11**

Paper 1 **October/November 2023**

MARK SCHEME

Maximum Mark: 80

**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2023 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.





**[Turn over**

## Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

**Mathematics-Specific Marking Principles**

1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.

2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.

3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.

4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).

5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.

6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

### Types of mark

M Method marks, awarded for a valid method applied to the problem.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.

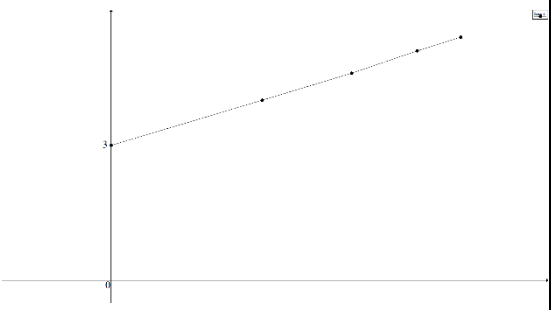
B Mark for a correct result or statement independent of Method marks.

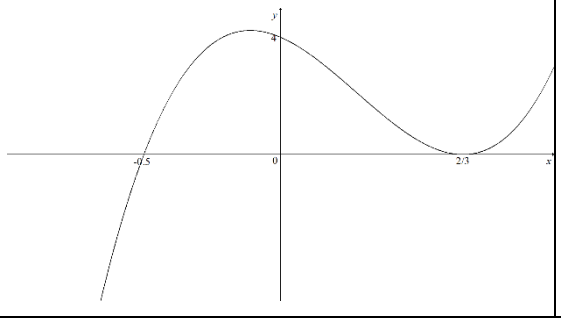
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

### Abbreviations

awrt answers which round to
cao correct answer only
dep dependent
FT follow through after error
isw ignore subsequent working
nfww not from wrong working
oe or equivalent
rot rounded or truncated
SC Special Case
soi seen or implied

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 1 | $a=4$ | **B1** | |
| | $b=3$ | **B1** | |
| | $c=-5$ | **B1** | |
| 2(a) | $c=0$ | **B1** | |
| | $\mathrm{P}\left(-\frac{1}{2}\right)$: $a+4b=-34$ oe | **B1** | Allow multiples but must be in terms of $a$, $b$ and one numeric term. |
| | $\mathrm{P}'(x)=3ax^2-22x+b$<br>$\mathrm{P}'(2)=12a-44+b$ soi | **M1** | For attempt to differentiate and substitute in $x=2$ |
| | $12a+b=62$ | **A1** | Allow multiples but must be in terms of $a$, $b$ and one numeric term. |
| | $a=6,\ b=-10$ | **2** | **M1 dep** for attempt to solve *their* simultaneous equations.<br>**A1** for both |
| 2(b) | $x\left(6x^2-11x-10\right)$ | **M1** | For $x\left((\textit{their } a)x^2-11x+\textit{their } b\right)$ |
| | $x(3x+2)(2x-5)$ | **A1** | |
| 3(a) | $\pm\begin{pmatrix}-5\\12\end{pmatrix}$ | **B1** | |
| | $\begin{pmatrix}-5\\12\end{pmatrix}$ | **B1** | |
| 3(b) | 13 | **B1** | **FT** on *their* (a) |
| 3(c) | $3\left(\textit{their } \overrightarrow{AB}\right)=2\overrightarrow{OX}-2\begin{pmatrix}2\\-6\end{pmatrix}$ | **M1** | Condone $3\left(\textit{their } \overrightarrow{AB}\right)=2\begin{pmatrix}2\\-6\end{pmatrix}-2\overrightarrow{OX}$ |
| | $\begin{pmatrix}-\frac{11}{2}\\12\end{pmatrix}$ | **A1** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 4(a) | $\ln y = \ln A + b \ln x$ soi | **B1** | May be implied by parts **(b)** and **(c)** |
| | <table><tr><td>$\ln x$</td><td>0</td><td>0.69</td><td>1.1</td><td>1.4</td><td>1.6</td></tr><tr><td>$\ln y$</td><td>3</td><td>4</td><td>4.6</td><td>5.1</td><td>5.4</td></tr></table>  | **2** | **M1** for attempt to plot a correct graph, allow one point error on the graph.<br>**A1** All points correct on the graph. |
| 4(b) | Vertical intercept = $\ln A$ $(=3)$ | **M1** | **Dep** on a straight line graph |
| | 20 | **A1** | |
| | Gradient = $b$ | **M1** | **Dep** on a straight line graph |
| | $b = 1.5$ (allow 1.4 to 1.6) | **A1** | |
| 4(c) | Reading off graph for $\ln x = 1.25$ to obtain $\ln y$<br>or use of *their* equation | **M1** | **Dep** on a straight line graph |
| | $120 \leqslant y \leqslant 150$ | **A1** | |
| 5(a)(i) | 5040 | **B1** | |
| 5(a)(ii) | 2520 | **B1** | |
| 5(a)(iii) | There are 504 codes less than 1000<br>$5040 - 504 = 4536$ | **2** | **M1** for *their* **(i)** $-504$ or $9 \times$ (a product of 3 relevant numbers) |
| 5(b) | With family: 462 | **B1** | |
| | Without family: 55 | **B1** | |
| | Total: 517 | **B1** | |
| 6(a) | $\lg 50x^3$ | **3** | **B1** for $\lg x^3$ or $\lg 2$ or $\lg 100$<br>**B1** for $\lg \frac{x^3}{2}$ |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 6(b) | $\log_4 a = \dfrac{1}{\log_a 4}$ | **B1** | |
| | $2(\log_a 4)^2 - 5\log_a 4 - 3 = 0$ | **M1** | For attempt to obtain a 3-term quadratic equation in $\log_a 4$ and an attempt to solve to obtain $\log_a 4 = ...$ |
| | $\log_a 4 = -\dfrac{1}{2}$, $\log_a 4 = 3$<br>$a = \dfrac{1}{16}$, $a = 4^{\frac{1}{3}}$ oe | **3** | **M1 Dep** for dealing with logarithms correctly at least once, to obtain $a = \ldots$<br>**A1** for each correct solution nfww. |
| | **Alternative:** | | |
| | $\log_a 4 = \dfrac{1}{\log_4 a}$ | **(B1)** | |
| | $3(\log_4 a)^2 + 5\log_4 a - 2 = 0$ | **(M1)** | For attempt to obtain a 3-term quadratic equation in $\log_a 4$ and an attempt to solve to obtain $\log_a 4 = ...$ |
| | $\log_4 a = -2$, $3\log_4 a = 1$<br>$a = \dfrac{1}{16}$, $a = 4^{\frac{1}{3}}$ oe | **(3)** | **M1 Dep** for dealing with logarithms correctly at least once, to obtain $a = \ldots$<br>**A1** for each correct solution nfww. |
| 7(a) | $\dfrac{dy}{dx} = 2\times 3\times (2x+1)(3x-2) + 2(3x-2)^2$ | **2** | **M1** for attempt at differentiation of a product, allow one arithmetic error.<br>**A1** all correct, allow unsimplified. |
| | $2(3x-2)(9x+1)$ | **A1** | |
| 7(b) | $\left(\dfrac{2}{3},\ 0\right)$ | **B1** | Must be from a correct derivative |
| | $\left(-\dfrac{1}{9},\ \dfrac{343}{81}\right)$ or $\left(-\dfrac{1}{9},\ 4.23\right)$ | **B1** | |
| 7(c) |  | **3** | **B1** for a correct cubic shape with a maximum in the second quadrant.<br>**B1** for $-\dfrac{1}{2}$ and $\dfrac{2}{3}$, must have a cubic shape<br>**B1** for 4 must have a cubic shape |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 7(d) | $0 < k < \frac{343}{81}$ or $0 < k < 4.23$ | **2** | **B1** for critical values 0 and *their* 4.23 or $\frac{343}{81}$ |
| 8 | $4x^2 - 6x - 5 = 1 - 4x$ oe<br>$2x^2 - x - 3 = 0$ oe | **2** | **M1** for attempt to eliminate $y$ and simplify to a 3-term quadratic equation $= 0$.<br>**A1** for a correct equation. |
| | Correct attempt to solve *their* quadratic equation to obtain 2 values for $x$ or for $y$ | **M1** | |
| | $x = -1, \quad \frac{3}{2}$ | **A1** | |
| | $y = 5, \quad -5$ | **A1** | |
| | $\frac{dy}{dx} = 8x - 6$<br>When $x = \frac{3}{2}$, $\frac{dy}{dx} = 6$ | **M1** | For finding the value of $\frac{dy}{dx}$ using *their* $x = \frac{3}{2}$ |
| | Equation of tangent: $y = 6x - 14$ | **2** | **Dep M1** for attempt to find the equation of the tangent using *their* $x = \frac{3}{2}$ and *their* $y = -5$.<br>**A1** allow unsimplified. |
| | $5 = 6x - 14$ oe | **M1** | For use of *their* $y = 5$ in *their* tangent equation |
| | $x = 3.17$ | **A1** | |
| 9(a)(i) | $-3\tan\frac{\theta}{2} + 11\left(2\tan\frac{\theta}{2}\right) = \frac{19\sqrt{3}}{3}$ | **2** | **M1** for use of 12th term with *their* common difference.<br>**A1** allow unsimplified. |
| | $\tan\frac{\theta}{2} = \frac{\sqrt{3}}{3}$<br>$\theta = \frac{\pi}{3}$ | **2** | **Dep M1** for correct attempt to solve *their* $\tan\frac{\theta}{2} = \frac{\sqrt{3}}{3}$ |
| 9(a)(ii) | $\frac{10}{2}\left(2\left(-3\times\frac{\sqrt{3}}{3}\right) + 9\left(2\times\frac{\sqrt{3}}{3}\right)\right)$ oe | **M1** | For the use of the sum to 10 terms using *their* $\tan\frac{\theta}{2} = \frac{\sqrt{3}}{3}$ |
| | $20\sqrt{3}$ | **A1** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 9(b)(i) | Common ratio = $4\sin^2\phi$ | **B1** | |
| | $1+4\sin^2\phi=4$ | **M1** | For use of $1+$*their* $r=4$ |
| | $\sin\phi=\pm\frac{\sqrt{3}}{2}$<br>$\phi=\pm\frac{\pi}{3}$ | **2** | **M1** for a correct attempt to solve *their* $\sin\phi=\pm\frac{\sqrt{3}}{2}$ to obtain at least one solution. |
| 9(b)(ii) | Common ratio = 3 soi | **M1** | For attempt to find numerical value of *their* common ratio. |
| | $3>1$ so no sum to infinity [as $-1<r<1$ to have a sum to infinity.] oe | **A1** | Must have correct common ratio. |
| 10(a) | $\frac{(x-4)\left(\frac{1}{2}\times 6x\left(3x^2-2\right)^{-\frac{1}{2}}\right)-\left(3x^2-2\right)^{\frac{1}{2}}}{(x-4)^2}$ | **3** | **B1** for $\frac{1}{2}\times 6x\left(3x^2-2\right)^{-\frac{1}{2}}$, allow unsimplified.<br>**M1** for a correct attempt to differentiate a quotient.<br>**A1** for all other terms correct. |
| | $\frac{\left(3x^2-2\right)^{-\frac{1}{2}}}{(x-4)^2}\left(3x(x-4)-\left(3x^2-2\right)\right)$ | **M1** | For a correct attempt to simplify to obtain the given form. |
| | $\frac{-12x+2}{\sqrt{3x^2-2}(x-4)^2}$ | **A1** | |
| 10(b) | When $x=3$, $\frac{dy}{dx}=\frac{-36+2}{5}$ | **M1** | For attempt using *their* $\frac{dy}{dx}$ |
| | $-6.8h$ | **2** | **Dep M1** for attempt at small changes using their $-6.8$.<br>**A1** cao |