



Cambridge International AS & A Level

CANDIDATE
NAME

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CENTRE
NUMBER

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FURTHER MATHEMATICS

9231/13

Paper 1 Further Pure Mathematics 1

May/June 2023

2 hours

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Any blank pages are indicated.

- (d) Given that $k = 2\sqrt{3}$ and $\theta = \frac{1}{3}\pi$, show that the invariant points of the transformation represented by \mathbf{M} lie on the line $3y + \sqrt{3}x = 0$. [4]

5 (a) Show that the curve with Cartesian equation

$$x^2 - y^2 = a,$$

where a is a positive constant, has polar equation $r^2 = a \sec 2\theta$. [3]

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The curve C has polar equation $r^2 = a \sec 2\theta$, where a is a positive constant, for $0 \leq \theta < \frac{1}{4}\pi$.

(b) Sketch C and state the minimum distance of C from the pole. [3]

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7 The curve C has equation $y = \frac{x^2 + 2x + 1}{x - 3}$.

(a) Find the equations of the asymptotes of C . [3]

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(b) Find the coordinates of the turning points on C . [3]

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(c) Sketch C .

[3]

(d) Sketch the curves with equations $y = \left| \frac{x^2 + 2x + 1}{x - 3} \right|$ and $y^2 = \frac{x^2 + 2x + 1}{x - 3}$ on a single diagram, clearly identifying each curve. [4]

